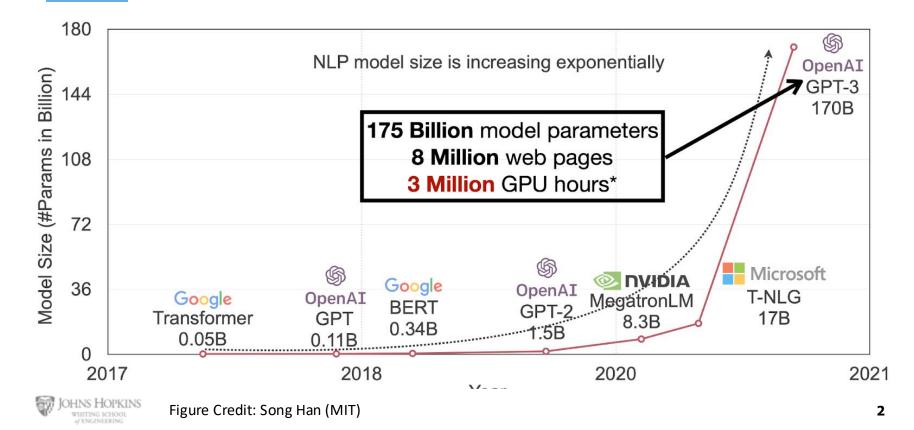


Model Efficiency

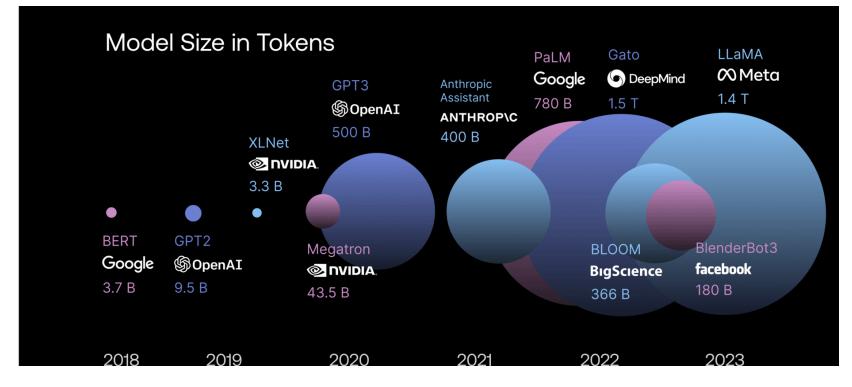
CSCI 601-471/671 (NLP: Self-Supervised Models)

https://self-supervised.cs.jhu.edu/sp2025/

Our models are getting larger!



And consumes a lot of data!





Motivation

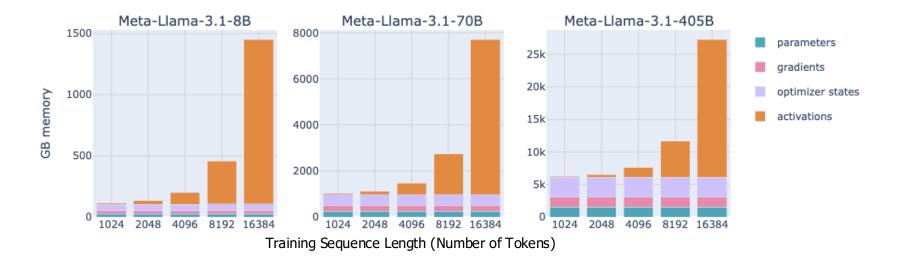
How much GPU memory (at least) do we need to perform inference/training? (batch size=1, ignoring the KV cache)

Model Size (Llama 3 Arch)	Inference Memory (~2x model size)	Training Memory (~7x model size)
8B	16GB	6oGB
70B	140GB	500GB
405B	810GB	3.25TB



Where did all the memory go?

Longer sequences require much more memory in training!

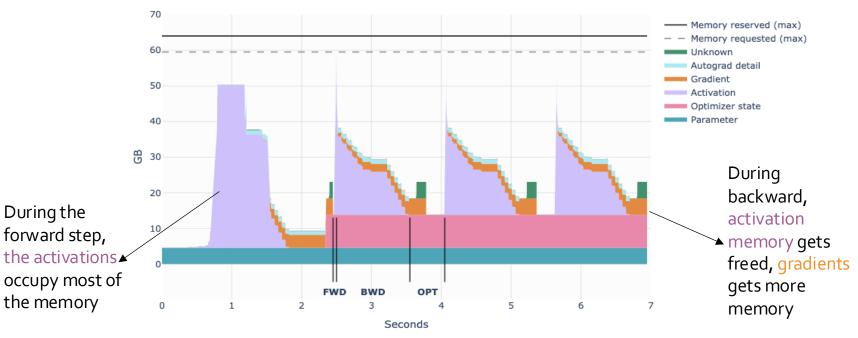


Source: https://nanotron-ultrascale-playbook.static.hf.space/dist/index.html



Memory consumption is not static

Memory profile of the first 4 training steps of Llama 1B



Source: https://nanotron-ultrascale-playbook.static.hf.space/dist/index.html



Model Efficiency: Topics

1. Distributed Training

2. Quantization (Post Training Quantization)

3. Distillation

Chapter goal: Getting comfortable with various mathematical and systems foundations for efficient deployment of LLMs.

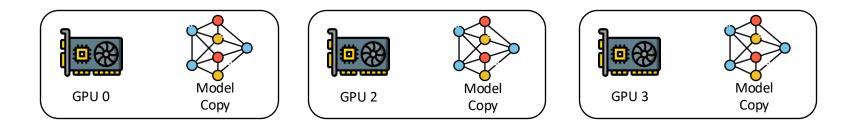


Distributed Training

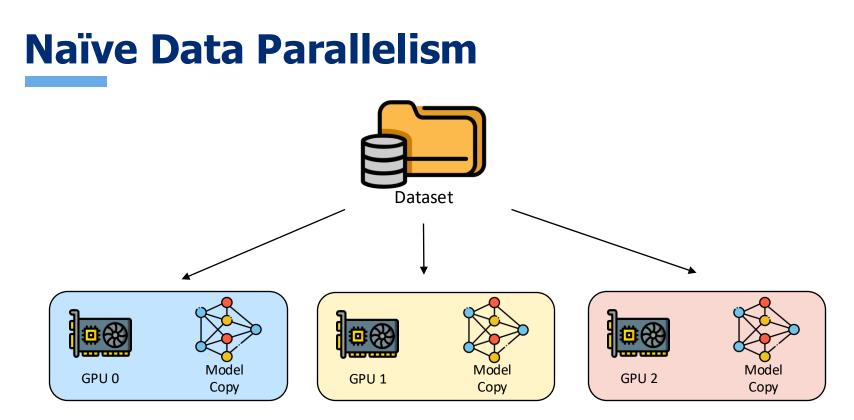


Distributed Training

- 1. Naïve Data Parallelism
- 2. Sharding Optimizer States (ZeRO, FSDP)
- 3. Model Parallelism (Tensor Parallelism, Pipeline Parallelism)



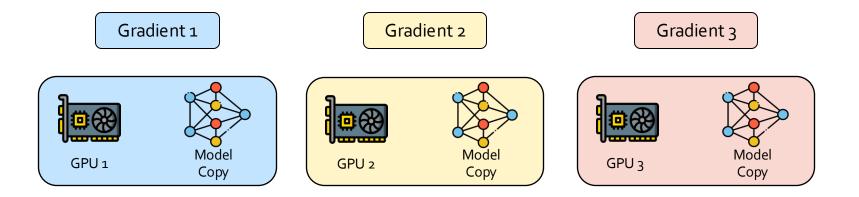




First, we want to shard the dataset and feed them into different GPUs How do we update the parameters?

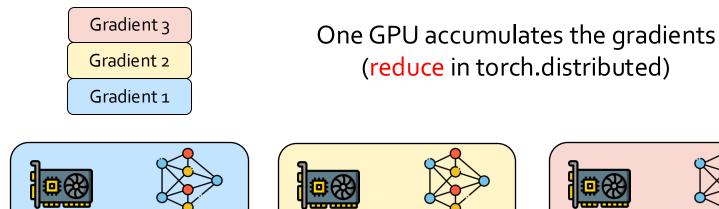
Naïve Data Parallelism

Each GPU compute gradient with a single shard of data





Naïve Data Parallelism



GPU 2

Model

Copy

GPU 3 Model Copy

Model

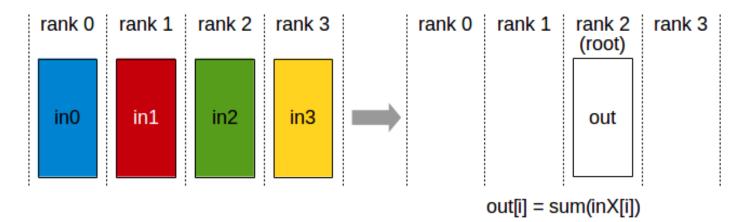
Copy



GPU 1

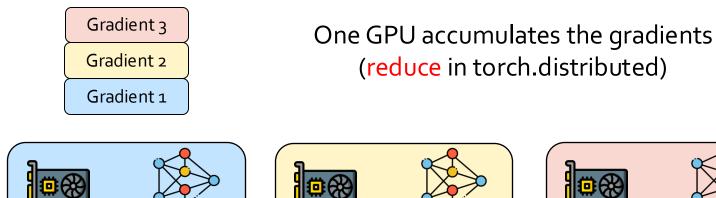
NCCL Operations: Reduce

- Nvidia Collective Communications Library (NCCL) A library developed to provide inter-GPU communications primitives (operations)
- Reduce: *Sums* over all *tensors* and stores it in a root GPU





Naïve Data Parallelism



Model

Copy

GPU 3 Model Copy

Model

Copy

GPU 2

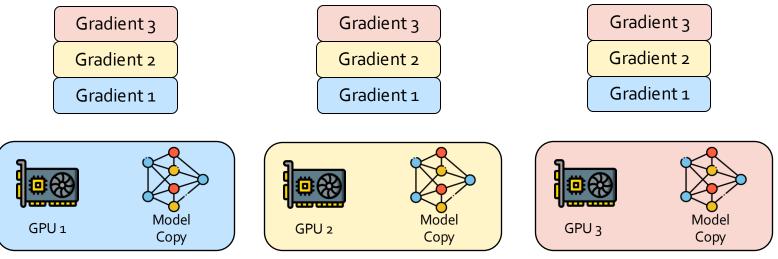


GPU 1



Naïve Data Parallelism

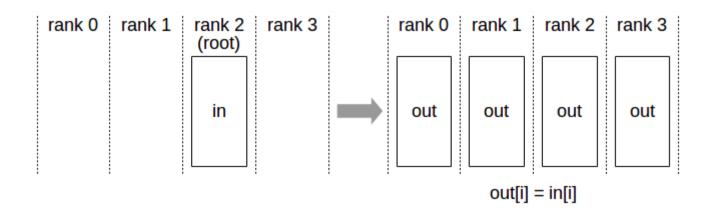
And send the accumulated gradient to all other GPUs (broadcast in torch.distributed)





NCCL Operations: Broadcast

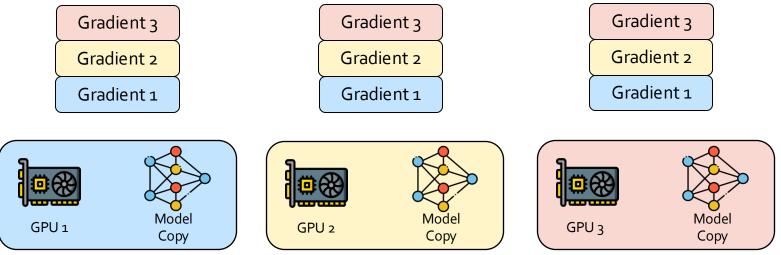
Broadcast: Duplicates one tensor to all GPUs





Naïve Data Parallelism

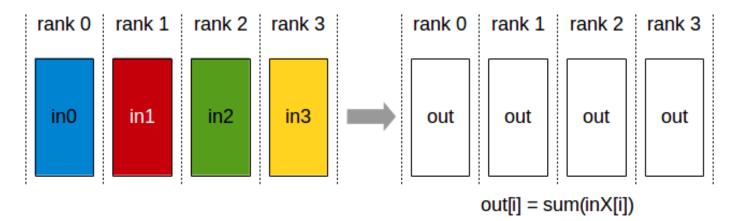
Accumulate gradients across all GPUs and perform gradient updates (all_reduce in torch.distributed)





NCCL Operations: All Reduce

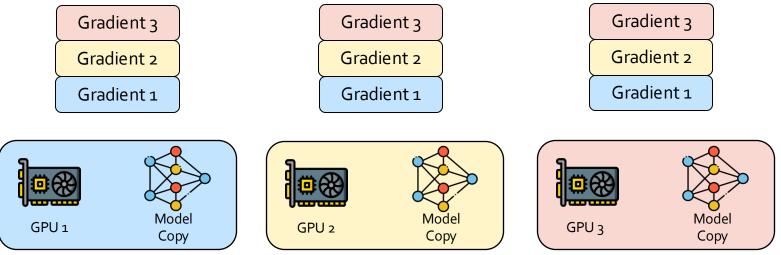
- All Reduce = Reduce + Broadcast
 - = Sum over input tensors, then duplicate it to all GPUs





Naïve Data Parallelism

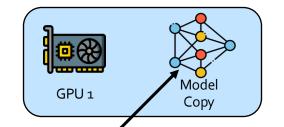
Accumulate gradients across all GPUs and perform gradient updates (all_reduce in torch.distributed)





What is wrong with Naïve DP

- Consumes too much memory in each GPU!



We need to store 5 copies of weights, / which occupies 16 bytes per param

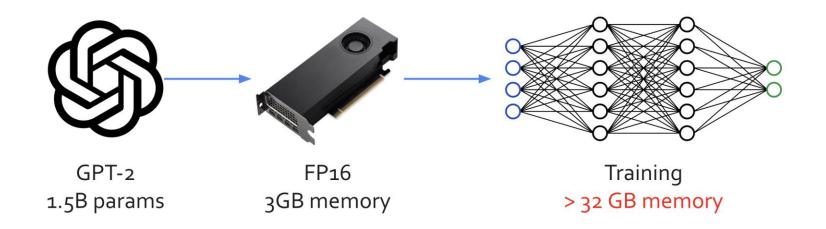
- 2 bytes for FP/BF16 model params
- 2 bytes for FP/BF16 gradients
- 4 bytes for FP32 master weights

(the thing you accumulate into in SGD, used in mixed precision training)

- 4 bytes for FP32 Adam first order estimates
- 4 bytes for FP32 Adam second order estimates

Slide Credit: Tatsunori Hashimoto (Stanford)

What is wrong with Naïve DP

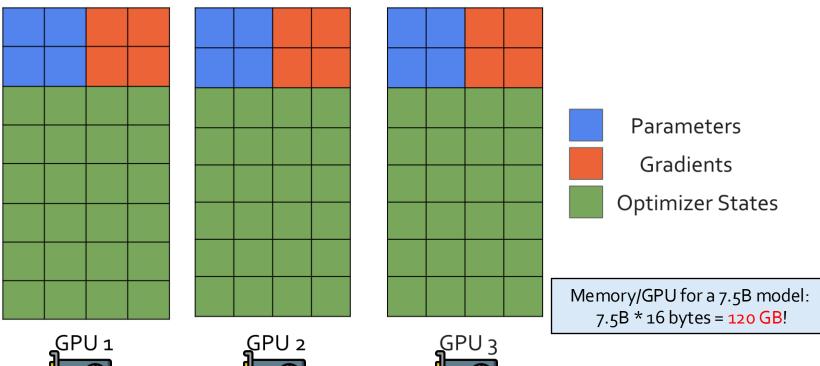


Most of the memory are occupied by optimizer states.

Some are also occupied by *residual states*: activations, buffers and fragmented memory

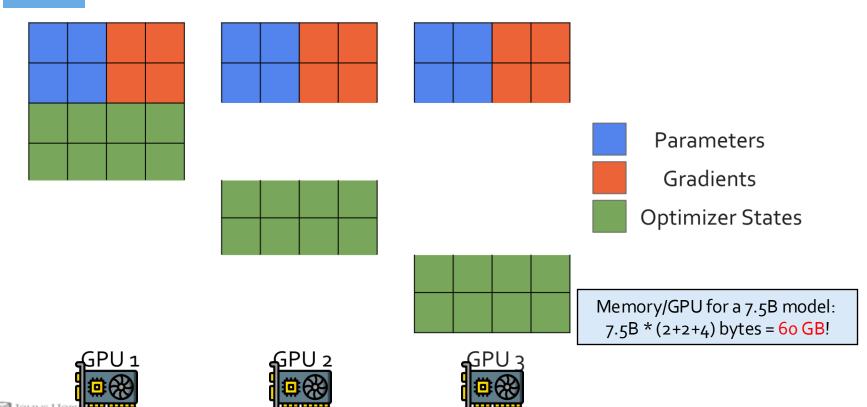


Naïve DP – Requires too much memory!



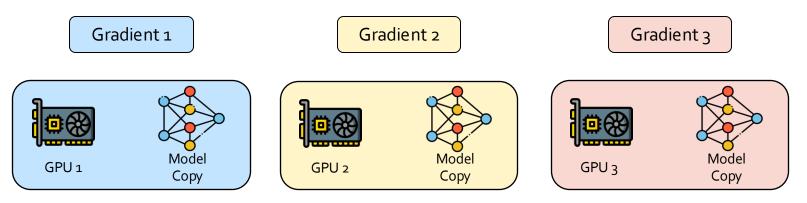


ZeRO Stage 1: Sharding Optimizer States



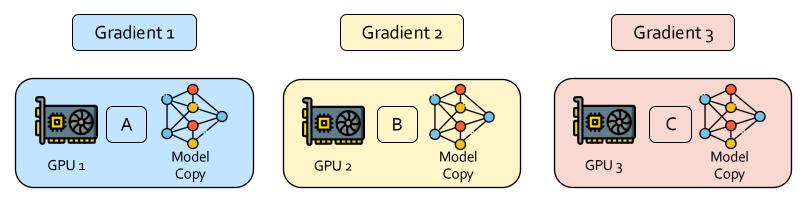
Update Parameters

Each GPU compute gradient with a single shard of data (The same as naïve DP)

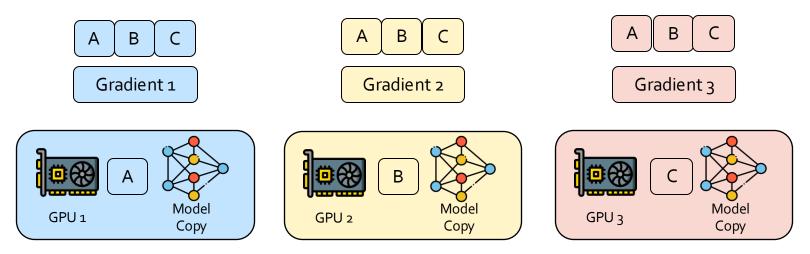


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Assuming that GPU1 stores parameter states for parameters A, GPU2 stores states for params B, GPU3 stores states for params C

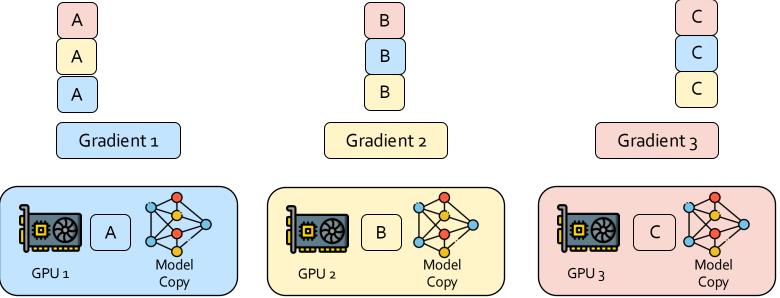


Split / shard the gradients into 3 parts!



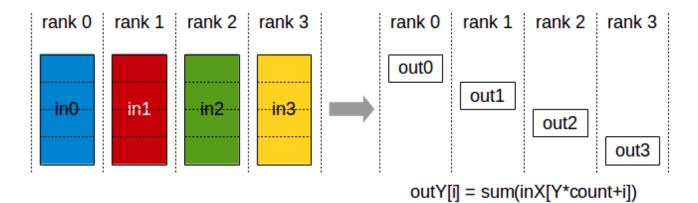
ZeRO: Memory Optimizations Toward Training Trillion Parameter Models (Rajbhandari et al., 2019) 26

Each GPU accumulates gradients of the params whose optimizer states the GPU is storing (reduce_scatter in torch.distributed)



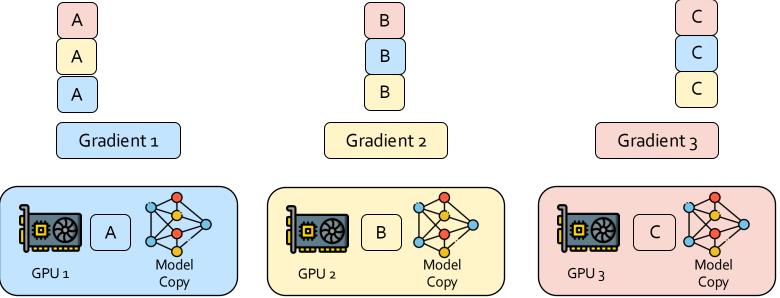
NCCL Operations: Reduce Scatter

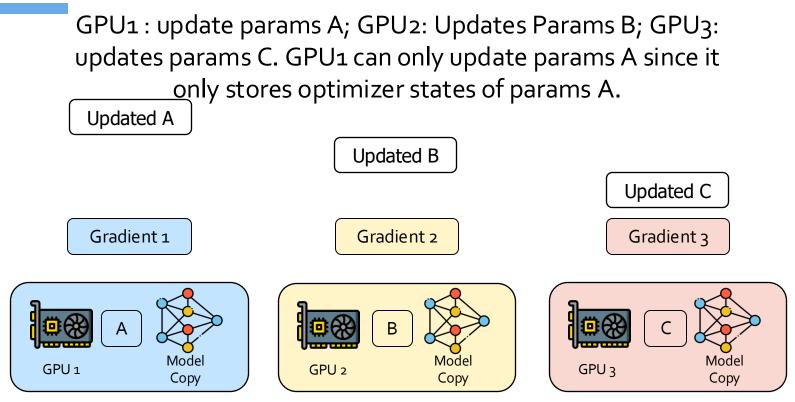
- reduce_scatter: each GPU stores the sum of <u>a shard</u> of the input.
- all_reduce: one GPU stores the sum over <u>all</u> the input.



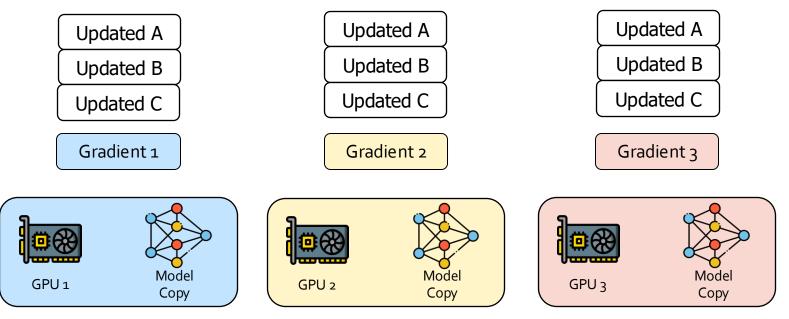


Each GPU accumulates gradients of the params whose optimizer states the GPU is storing (reduce_scatter in torch.distributed)





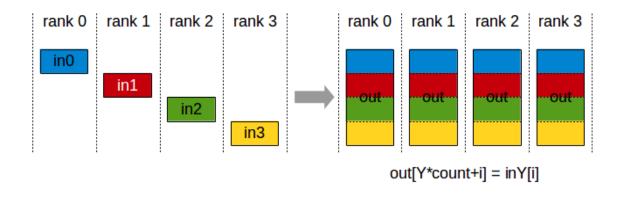
Each GPU sends updated params to every other GPU. Finishing optimizer.step(). (all_gather in torch.distributed)



ZeRO: Memory Optimizations Toward Training Trillion Parameter Models (Rajbhandari et al., 2019) 31

Quiz: NCCL Operations: All Gather

all_gather: every GPU performs a ____? operation in parallel.

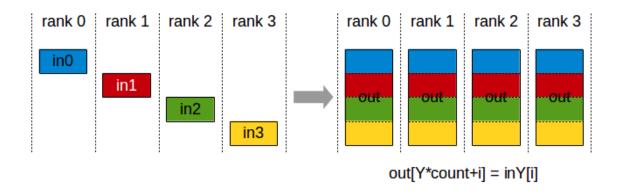


A.Reduce B. Broadcast C. Reduce_scatter



NCCL Operations: All Gather

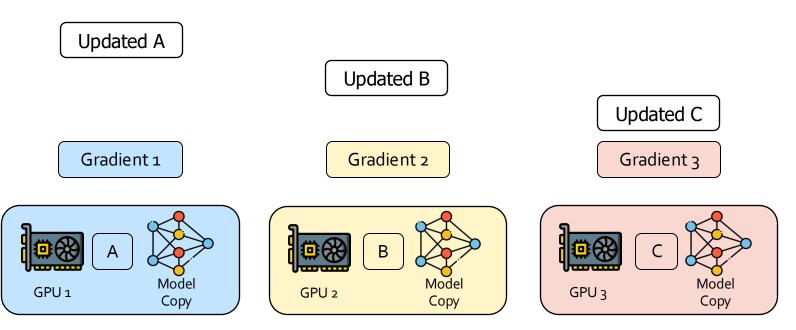
all_gather: every GPU performs a <u>broadcast</u> operation in parallel.



A.Reduce B. Broadcast C. Reduce_scatter

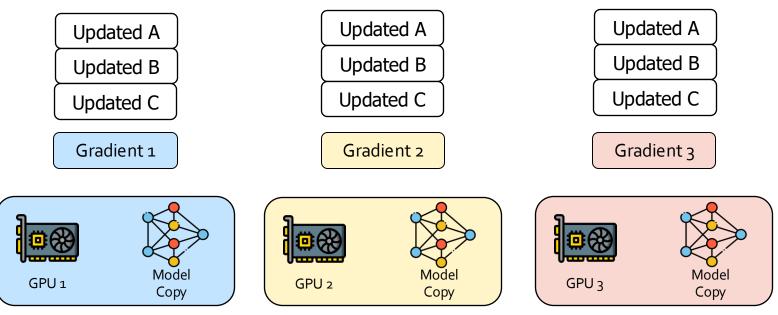


Before all_gather



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After all_gather, every GPU has a updated copy of the model



JOHNS HOPKINS WHITING SCHOOL «("ENGINEERING

ZeRO: Memory Optimizations Toward Training Trillion Parameter Models (Rajbhandari et al., 2019) 35

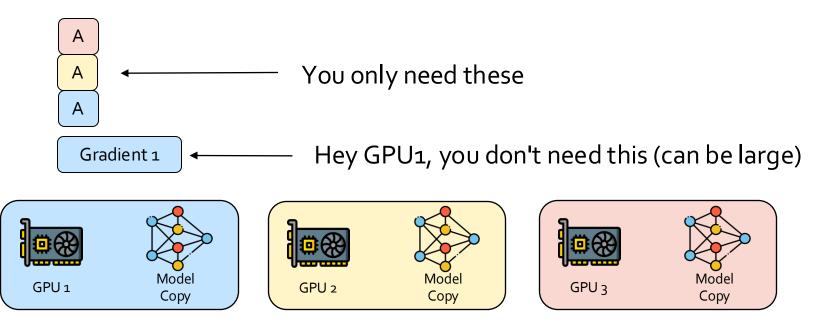
Summary: ZeRO 1

- reduce_scatter on the gradients: splitting the gradients into different GPUs
- Each GPU individually perform gradient updates
- all_gather on updated parameters
- Basically free! (Compared to Naïve Data Parallelism)

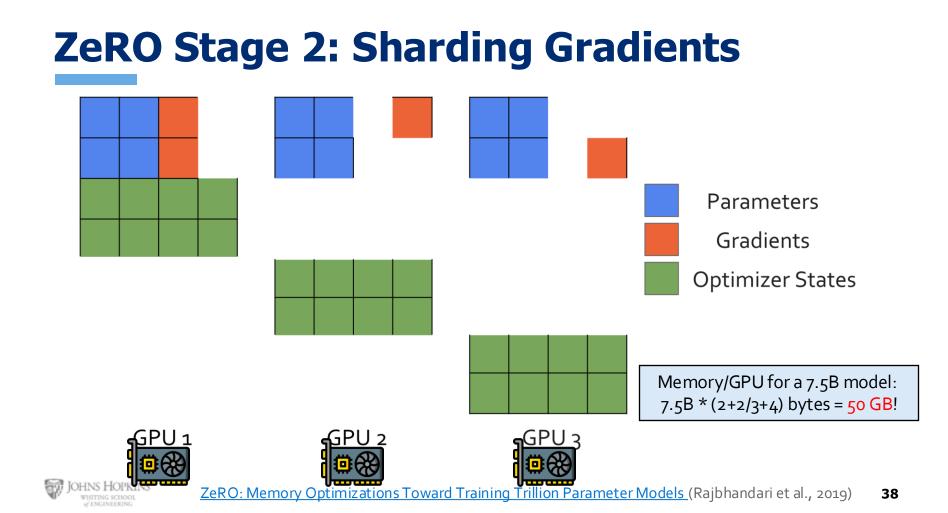


ZeRO Stage 1: How it works

Notice: Aside from the forward pass, GPU 1 only needs gradients A, but in fact it stores A and B and C

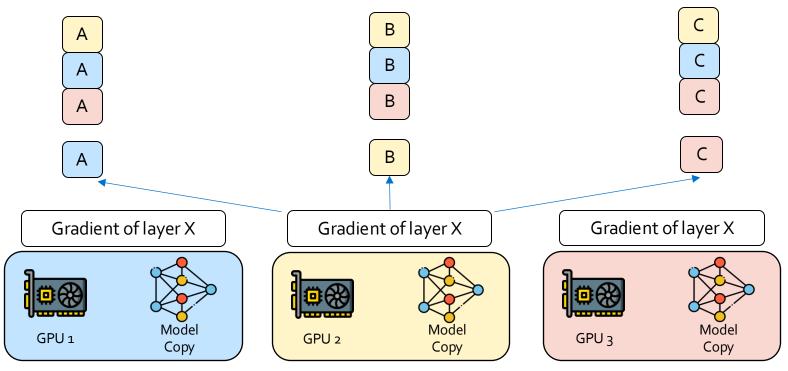


ZeRO: Memory Optimizations Toward Training Trillion Parameter Models (Rajbhandari et al., 2019) 37



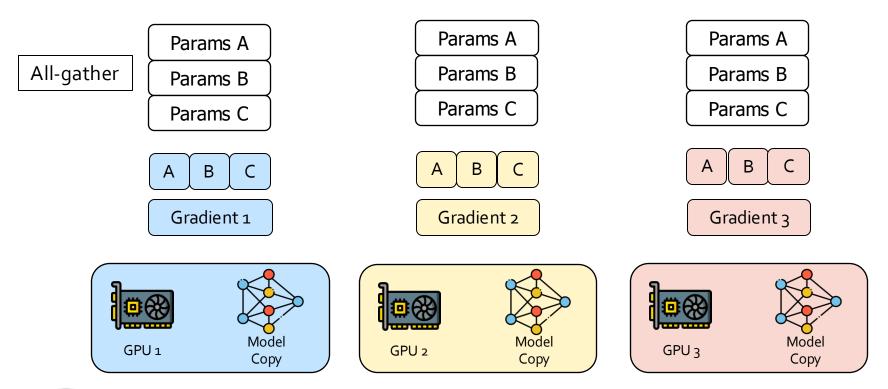
ZeRO Stage 2: How it works

Splitting the gradient of a single layer during backprop, then immediately shard it!



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ZeRO Stage 2: How it works



HNS HOPKINS

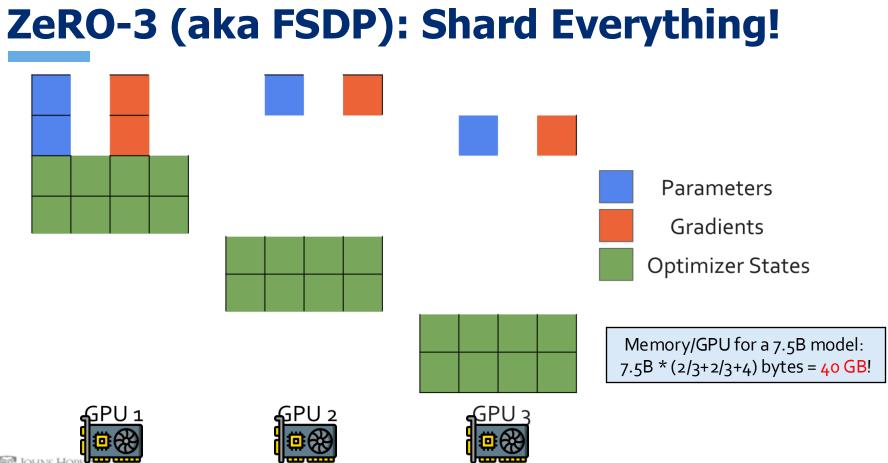
ZeRO: Memory Optimizations Toward Training Trillion Parameter Models (Rajbhandari et al., 2019)

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Summary: ZeRO 12

- reduce_scatter on the gradients: splitting the gradients into different GPUs
- Calculate gradients layer by layer and perform reduce_scatter, once layer is done, free the gradient
- Each GPU individually perform gradient updates
- all_gather on updated parameters
- Almost free!

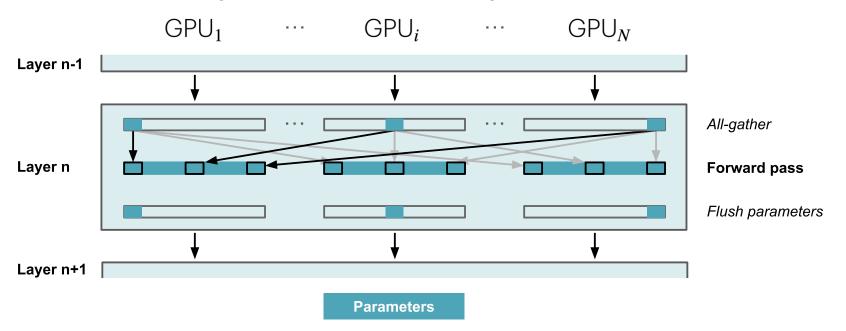




ZeRO: Memory Optimizations Toward Training Trillion Parameter Models (Rajbhandari et al., 2019) 42

ZeRO Stage 3: How it works (simplified)

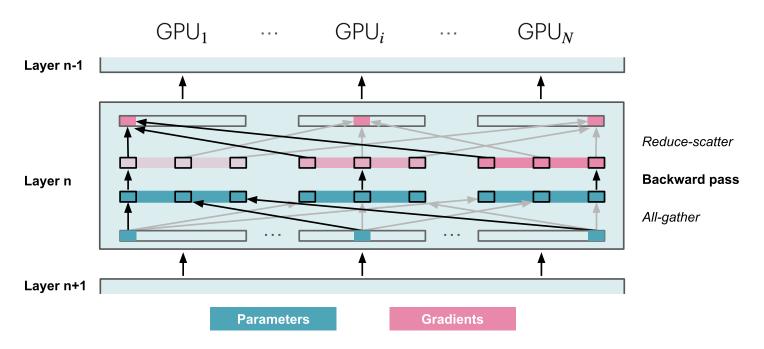
During forward pass, the parameters are gathered on-demand





ZeRO Stage 3: How it works (simplified)

During backward pass, the gradients are scattered (Reduce_Scatter)





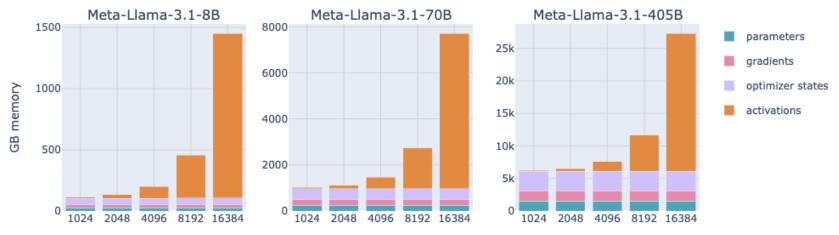
Communication Costs

- Naïve Data Parallel: 2x parameter (all_reduce)
- ZeRO-1: 2x parameter (reduce_scatter + all_gather) this is free! Might as well always use it.
- ZeRO-2: 2x parameter (reduce_scatter + all_gather + overhead) this is (almost) free!
- ZeRO-3: 3x parameter which can be quite slow.



Where did all the memory go?

So far, we dealt with the optimizer states but what about the activations?



Training Sequence Length (Number of Tokens)

Source: https://nanotron-ultrascale-playbook.static.hf.space/dist/index.html



Prefix Caching

but what about the activations?

<System> You are a helpful assistant ... <System> <User> I want to know how can I use the coffee machine <User>

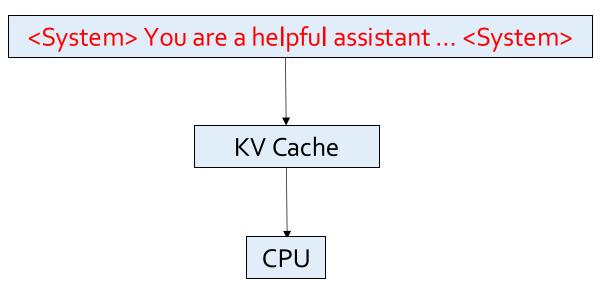
<System> You are a helpful assistant ... <System> <User> Write the code for training my language model. <User>

<System> You are a helpful assistant ... <System> <User> Help me revise my email ... <User>



Prefix Caching

Storing the activations in CPU and retrieve it when needed.



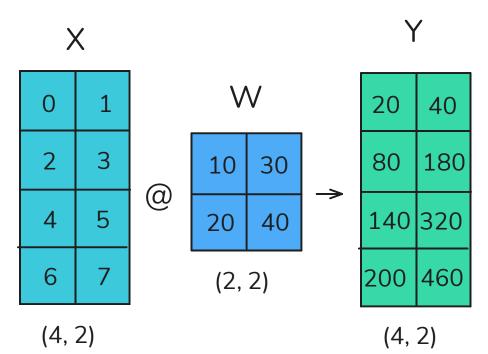
But, can we slice the activations to fit them in different GPUs?Yes, by Tensor Parallelism



Tensor Parallelism

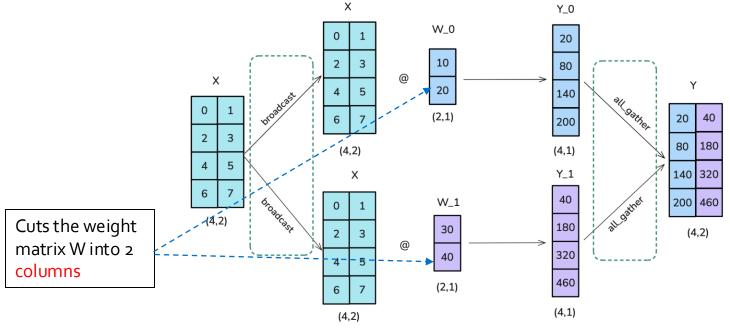
We can either cut the weights W into two columns (Column Parallelism)

or into two rows (Row Parallelism)





Column-wise Tensor Parallelism

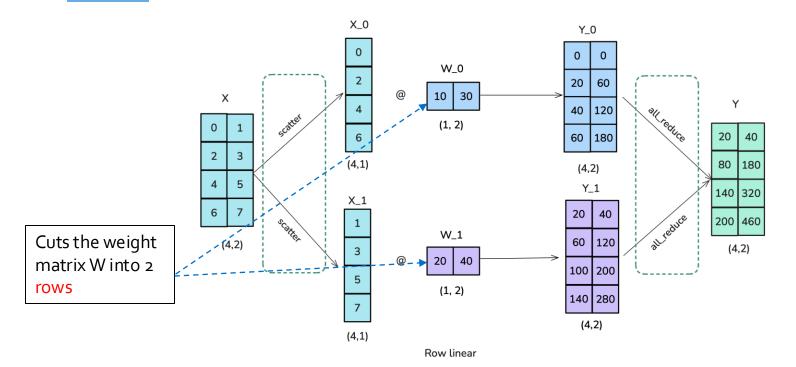


Column linear

Source: https://nanotron-ultrascale-playbook.static.hf.space/dist/index.html



Row-wise Tensor Parallelism



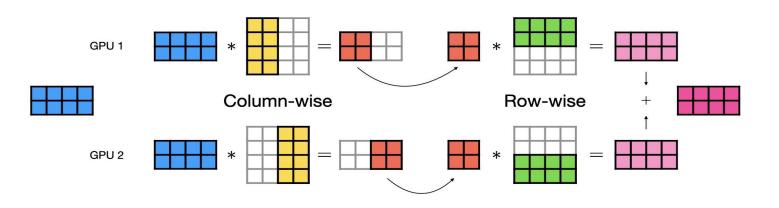
Source: https://nanotron-ultrascale-playbook.static.hf.space/dist/index.html



Tensor Parallelism

Computing matrix multiplications without storing internal activations (e.g. xW1)

In Feed-Forward Networks, The dimension of W1 is usually 4x the hidden dimension.





Tensor Parallelism: Llama Feed-Forward

```
self.w1 = ColumnParallelLinear(
       dim, hidden_dim, bias=False, gather_output=False, init_method=lambda x: x
   self.w2 = RowParallelLinear(
       hidden_dim, dim, bias=False, input_is_parallel=True, init_method=lambda x: x
   self.w3 = ColumnParallelLinear(
       dim, hidden_dim, bias=False, gather_output=False, init_method=lambda x: x
def forward(self, x);
   return self.w2(F.silu(self.w1(x)) * self.w3(x))
```

activations are element-wise operations, can be parallelized

Source: https://github.com/meta-llama/llama/blob/main/llama/model.py



Tensor Parallelism: Llama Attention

Column Parallel for Query, Key and Vector and Row Parallel for attention output

```
self.wg = ColumnParallelLinear(
    args.dim,
    args.n_heads * self.head_dim,
    bias=False,
    gather_output=False,
    init_method=lambda x: x,
self.wk = ColumnParallelLinear(
    args.dim,
    self.n_kv_heads * self.head_dim,
    bias=False,
    gather_output=False,
    init_method=lambda x: x,
self.wv = ColumnParallelLinear(
    args.dim,
    self.n kv heads * self.head dim,
    bias=False,
    gather_output=False,
    init method=lambda x: x,
```

self.wo = RowParallelLinear(
 args.n_heads * self.head_dim,
 args.dim,
 bias=False,
 input_is_parallel=True,
 init_method=lambda x: x,

Source: https://github.com/meta-llama/llama/blob/main/llama/model.py

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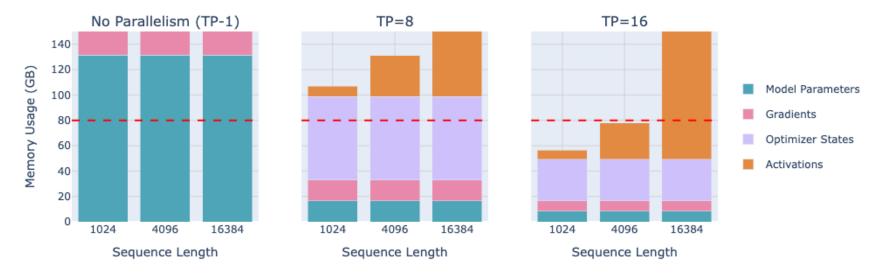
Summary so far

- Data Parallelism
 - Naïve Data Parallelism
 - NCCL Operations
 - (reduce, all_reduce, reduce_scatter, broadcast, all_gather)
 - ZeRO-1, ZeRO-2, ZeRO-3
- Prefix Caching
- Tensor Parallelism
 - Row-wise Tensor Parallelism
 - Column-wise Tensor Parallelism



Tensor Parallelism

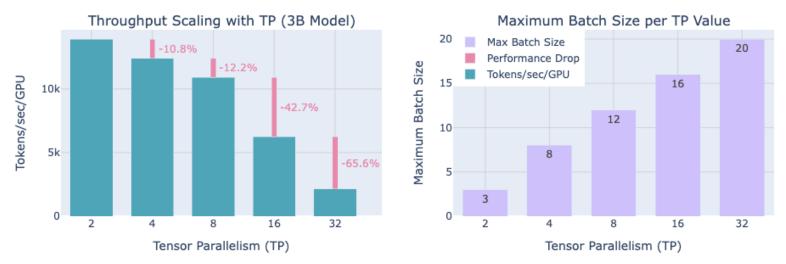
Memory Usage for 70B Model



Source: https://github.com/meta-llama/llama/blob/main/llama/model.py



Throughput Scaling of Tensor Parallelism



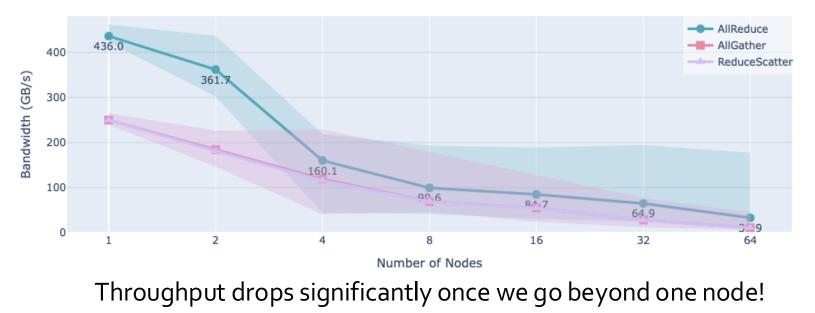
A large drop in throughput when scaling beyond 8 GPUs (one node)

Source: https://nanotron-ultrascale-playbook.static.hf.space/dist/index.html



Throughput Scaling of Tensor Parallelism

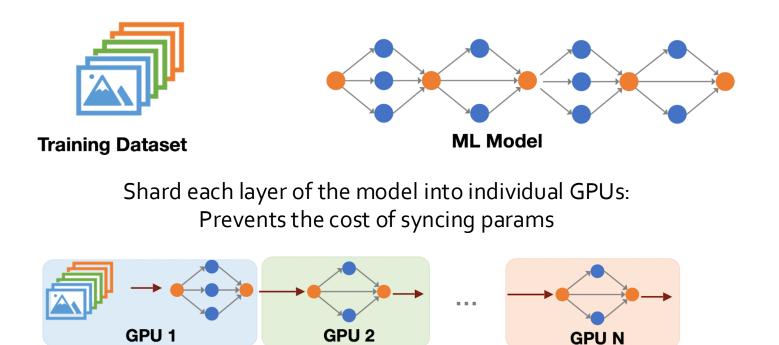
Communication Bandwidth by Number of Nodes (size=256MB)

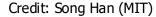


Source: https://nanotron-ultrascale-playbook.static.hf.space/dist/index.html



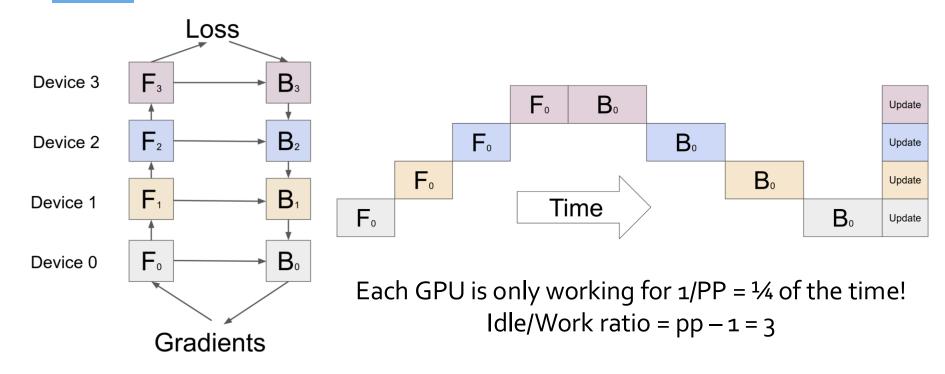
Pipeline Parallelism







Pipeline Parallelism



GPipe: Easy Scaling with Micro-Batch Pipeline Parallelism (Huang et al., NeurIPS 2019)

Pipeline Parallelism: Improvement

Solution: Splitting the data into mini-batches! (AFAB)

			F _{3,0}	F _{3,1}	F _{3,2}	F _{3,3}	B 3,3	B 3,2	B 3,1	B 3,0				Update
		F _{2,0}	F _{2,1}	F _{2,2}	F _{2,3}			B _{2,3}	B _{2,2}	B _{2,1}	B _{2,0}			Update
	F 1,0	F 1,1	F 1,2	F 1,3					B 1,3	B 1,2	B 1,1	B 1,0		Update
F _{0,0}	F _{0,1}	F _{0,2}	F 0,3			Bı	ubble	,		B 0,3	B _{0,2}	B _{0,1}	B 0,0	Update

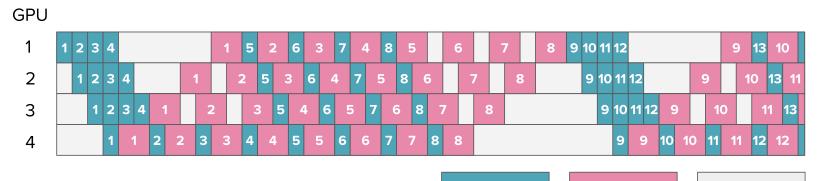
Idle / Work Ratio = PP-1/M=3/4

GPipe: Easy Scaling with Micro-Batch Pipeline Parallelism (Huang et al., NeurIPS 2019)



Pipeline Parallelism

A cleverer version of AFAB: 1 Forward 1 Backward (1F1B) Idea: Do backward as early as possible, releasing activations on the fly



Roughly the same Idle/Work Ratio but less memory (as you only need to store p=4 activations rather than m=8)

GPipe: Easy Scaling with Micro-Batch Pipeline Parallelism (Huang et al., NeurIPS 2019)

Forward pass

Backward pass

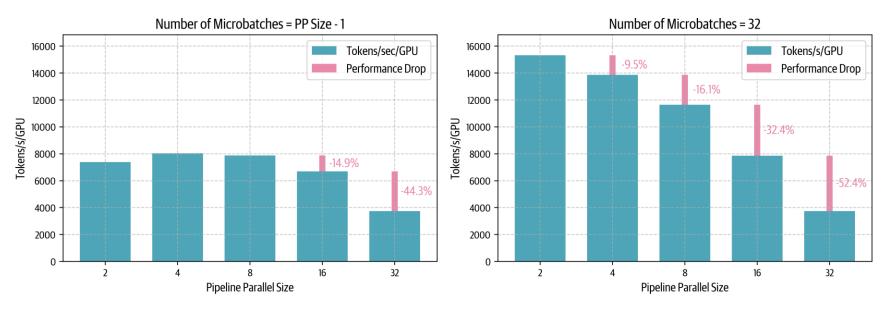


Time

Device idle

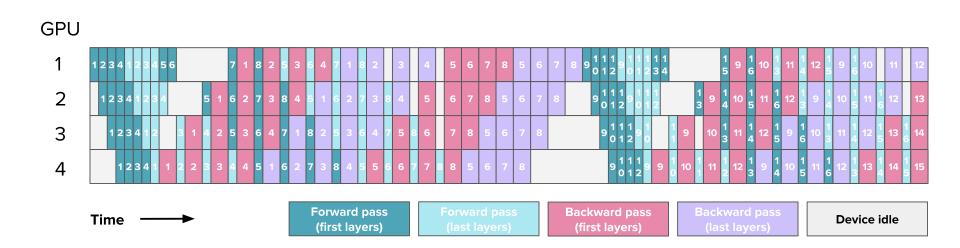
Pipeline Parallelism Throughput

Throughput Scaling with Pipeline Parallelism (1F1B schedule)



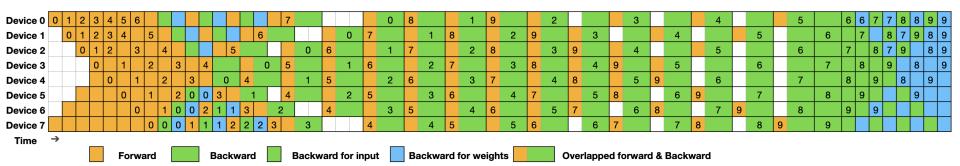
A small drop in throughput when scaling beyond 8 GPUs (one node) but a large drop as we increase the microbatch number

Interleaving Pipeline Parallelism (LLama3)





Interleaved Pipeline Parallelism (DeepSeek)

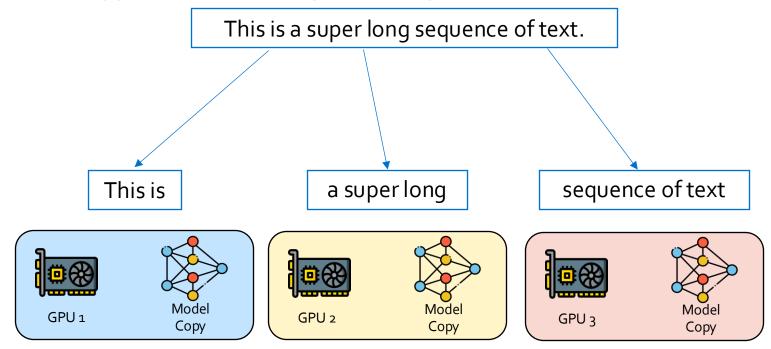


backprop for weights (blue) can be computed at any time! We fill in the bubble with weight back propagation.



What about (super) long sequences?

Suppose we want to split the sequence into different GPUs

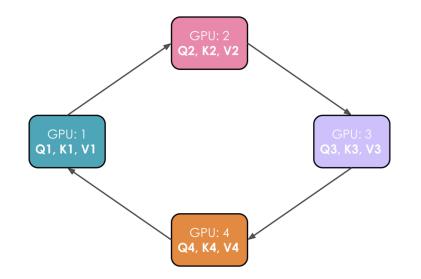


What about (super) long sequences?

 Feed Forward Network / LayerNorm is not affected by splitting the sequence, each token is processed individually

- But what about attention? Each token needs to compute dot product with every other token.





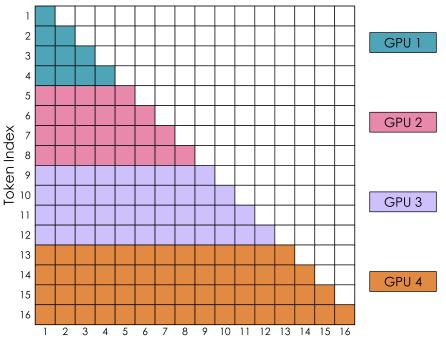
Just pass the Key, Value pairs around!

However, attention mask is usually causal – Q1 does not need K2, V2, ...

Source: Ring Attention with Blockwise Transformers For Near-Infinite Context (Liu et al., 2023)



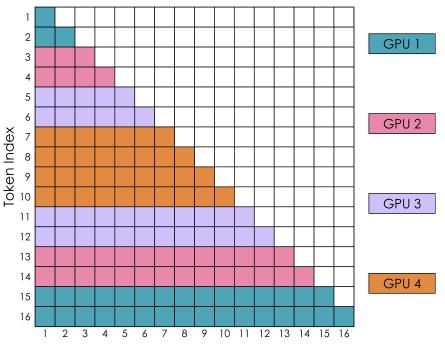
Causal Attention Mask



GPU 1 computes the presoftmax-ed scores for Q1, Q2, Q3, Q4.. then becomes idle.

Source: Ring Attention with Blockwise Transformers For Near-Infinite Context (Liu et al., 2023)

Causal Attention Mask

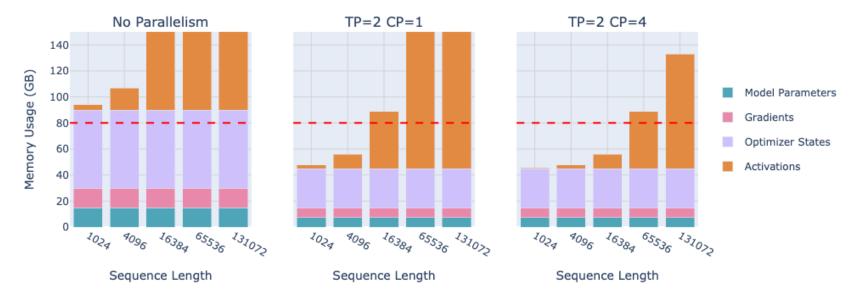


Balancing the workload for each individual GPUs.

Source: Striped Attention: Faster Ring Attention for Causal Transformers (Brandon et al., 2023)



Memory Usage for 8B Model



Source: https://nanotron-ultrascale-playbook.static.hf.space/dist/index.html



Summarizing

	Sync overhead	Memory	Bandwidth	Batch size	Easy to use?
DDP/ZeRO1	Per-batch	No scaling	2* # param	Linear	Very
FSDP (ZeRO3)	3x Per-FSDP block	Linear	3 * # param	Linear	Very
Pipeline	Per-pipeline	Linear	Activations	Linear	No
Tensor+seq	2x transformer block	Linear	8*activations per- layer all-reduce	No impact	No



Source: Tatsunori Hashimoto (Stanford)

Solutions

- DeepSeek V3: DP=1, PP=16, EP (Expert Parallelism) = 8

3.2 Training Framework

The training of DeepSeek-V3 is supported by the HAI-LLM framework, an efficient and lightweight training framework crafted by our engineers from the ground up. On the whole, DeepSeek-V3 applies 16-way Pipeline Parallelism (PP) (Qi et al., 2023a), 64-way Expert Parallelism (EP) (Lepikhin et al., 2021) spanning 8 nodes, and ZeRO-1 Data Parallelism (DP) (Rajbhandari et al., 2020).

- TP **TFLOPs/GPU** GPUs CP PP DP Seq. Len. Batch size/DP Tokens/Batch BF16 MFU 43%8.192163216M8 1 648,19243016.384168,1921616M40041%8 1 12838%16,3848 16168 131,0721616M380
- Llama 3: Staged Training

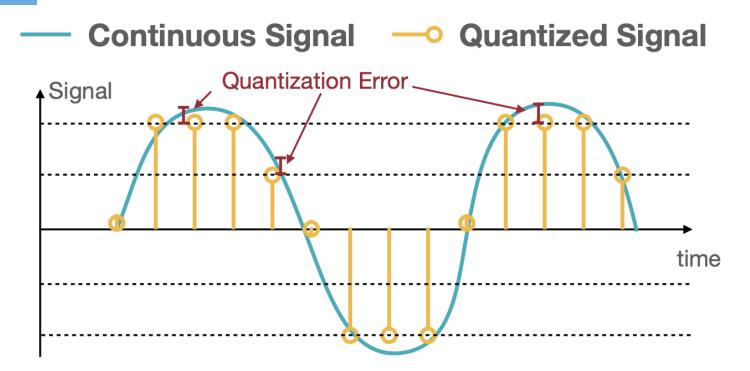
Table 4Scaling configurations and MFU for each stage of Llama 3 405B pre-training.See text and Figure 5 for descriptionsof each type of parallelism.



Quantization



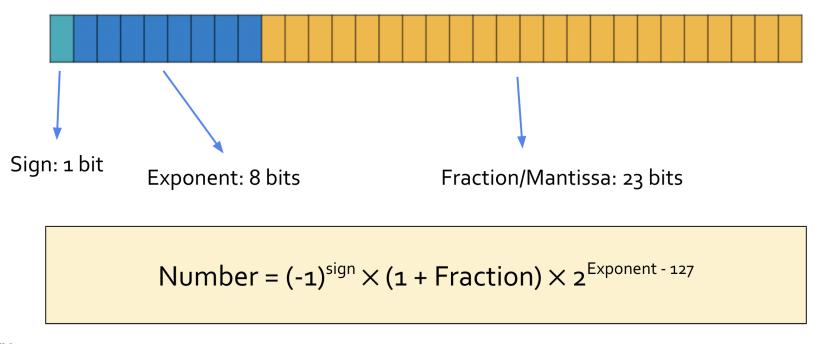
Quantization: Mapping from high to low precision

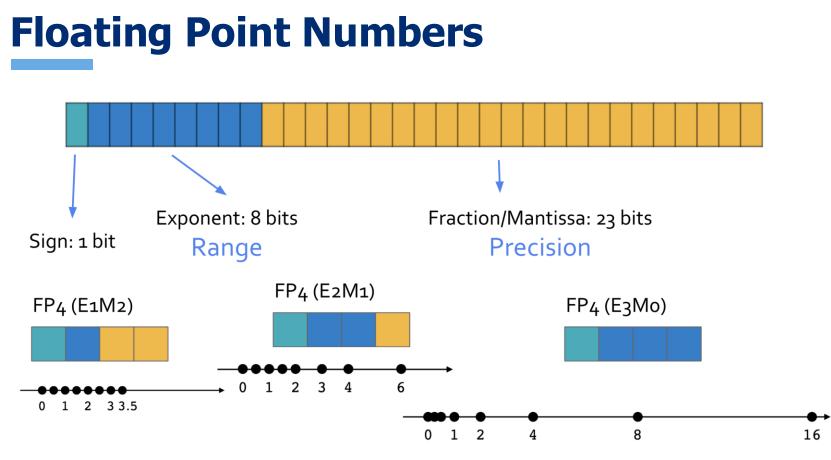




Numeric Data Types

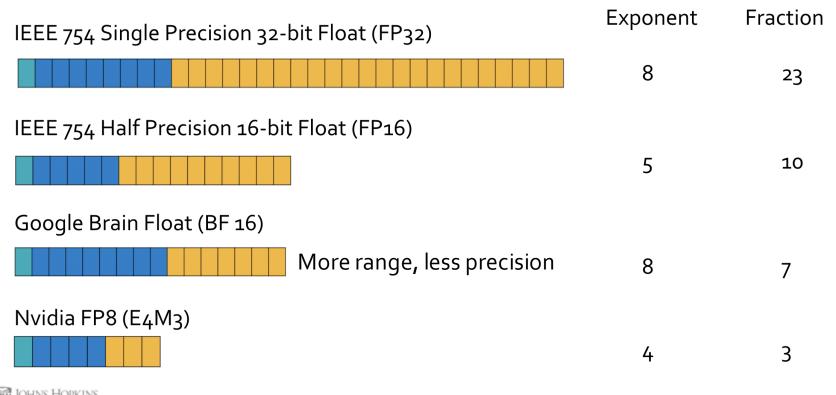
Example: 32-bit floating point number in IEEE 754 (FP32)



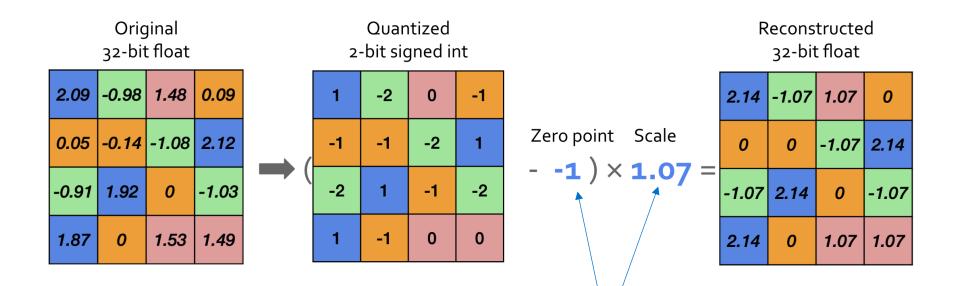




Floating Point Numbers



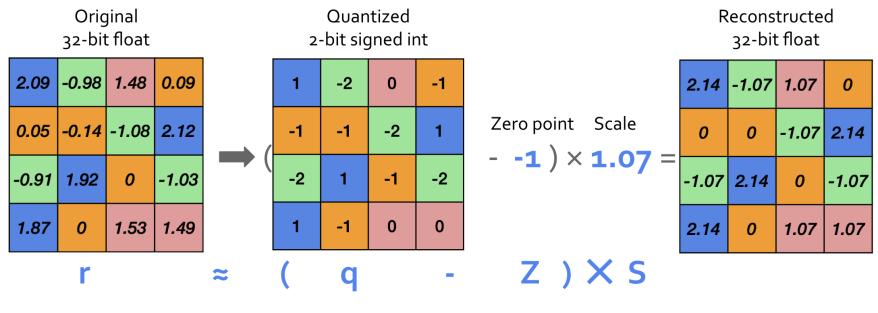
Linear Quantization



How to find these numbers?



Linear Quantization



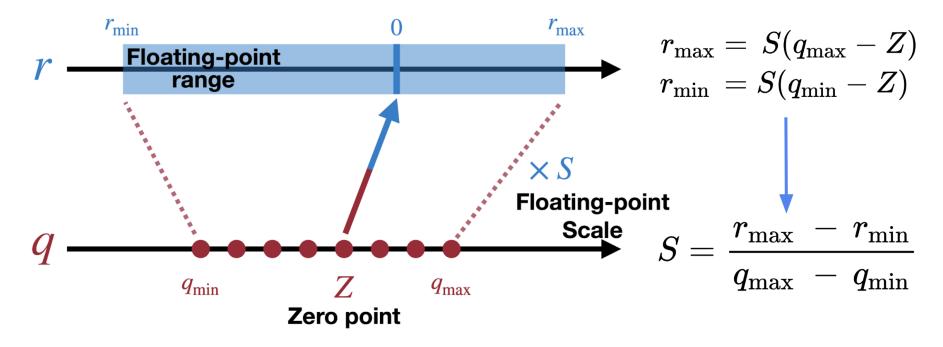
floating-point

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integer

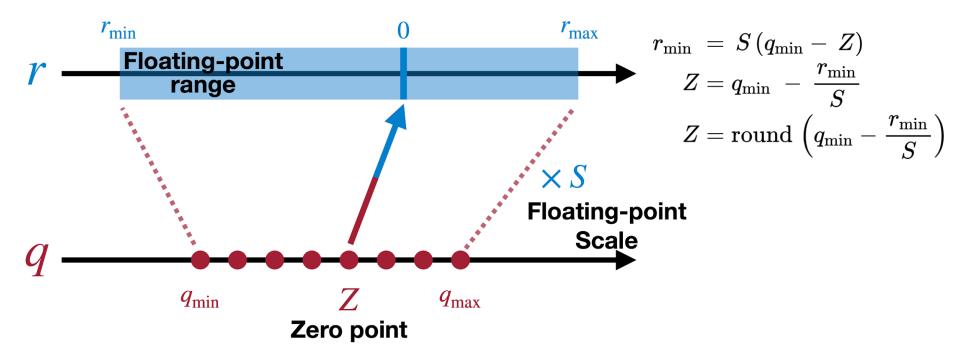
integer floating-point

Linear Quantization: Scale



Quantization and Training of Neural Networks for Efficient Integer-Arithmetic-Only Inference (Jacob et al., CVPR 2018)

Linear Quantization: Zero Point



Quantization and Training of Neural Networks for Efficient Integer-Arithmetic-Only Inference (Jacob et al., CVPR 2018)

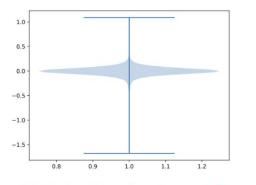


Linear Quantization: Zero Point

"Absmax" Implementation

In practice, the weights are usually centered around zero (Z = o):

Therefore, we can find scale by using only the max.



 $q_{ ext{max}} - q_{ ext{min}} \ igg| \ = rac{r_{ ext{min}}}{q_{ ext{min}} - Z} = rac{-|r|_{ ext{max}}}{q_{ ext{min}}}$

Tmax

S =

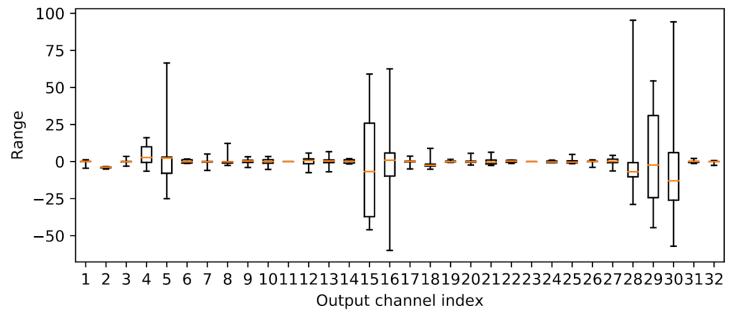
 $r_{\rm min}$

Used in Pytorch, ONNX

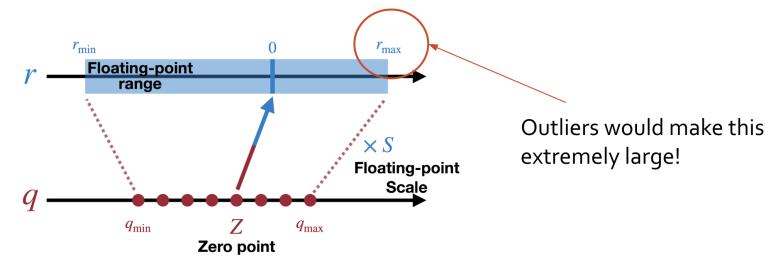
Weight distribution of first conv layer of ResNet-50.

Quantization and Training of Neural Networks for Efficient Integer-Arithmetic-Only Inference (Jacob et al., CVPR 2018) 83

There exists many outliers in activations (activations of the first layer MobileNetV2):

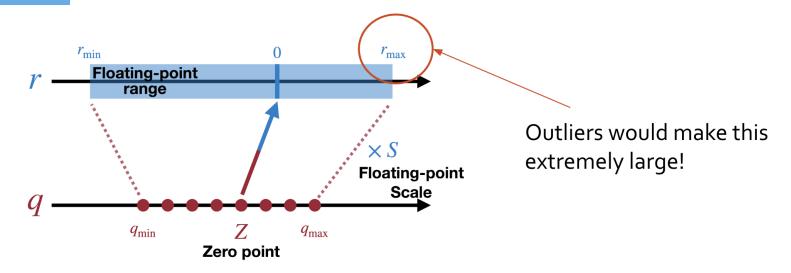






Example: 15, 0.1, 0.02, 1.0, 0.01 -> 127, 1, 0, 8, 0 (Everything under 0.05 gets mapped to 0)



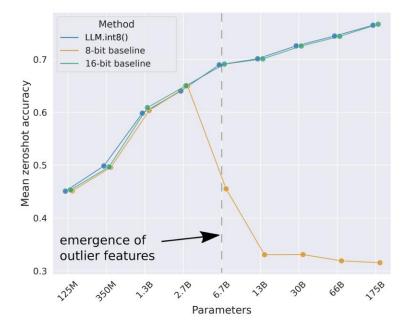


Example: 15, 0.1, 0.02, 1.0, 0.01 -> 127, 1, 0, 8, 0 (Everything under 0.05 gets mapped to 0)

Quantize each channel individually, each channel gets its own scale and Zero-point!

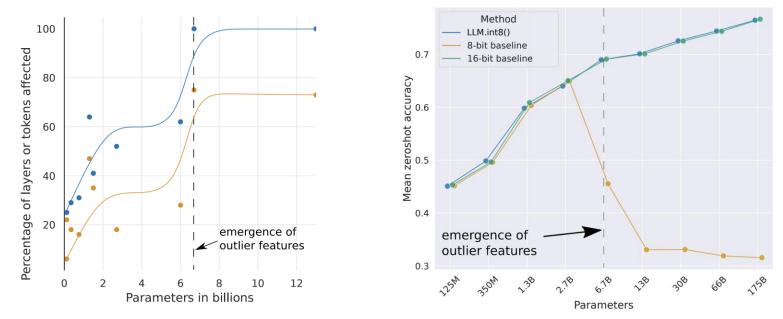
Data-Free Quantization Through Weight Equalization and Bias Correction (Kagel et al., ICCV 2019) 86

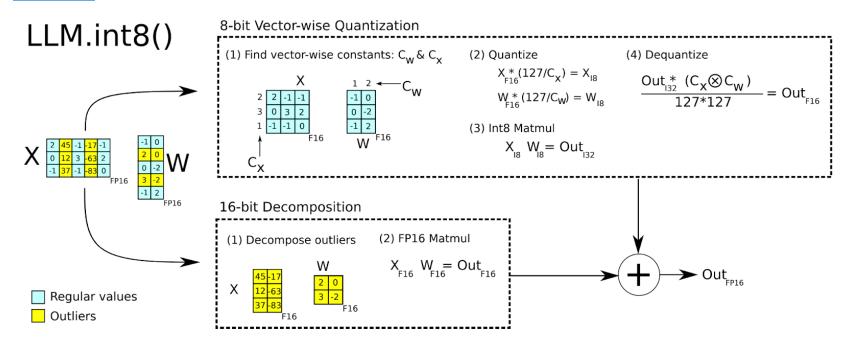
Outlier features significantly harms performance after quantization in LMs.





Outlier features significantly harms performance after quantization in LMs.





Keep outlier channels / features in 16-bit, quantize the rest.

LLM.int8(): 8-bit Matrix Multiplication for Transformers at Scale (Dettmers et al., NeurIPS 2022)

Parameters	125M	1.3B	2.7B	6.7B	13 B
32-bit Float	25.65	15.91	14.43	13.30	12.45
Int8 absmax	87.76	16.55	15.11	14.59	19.08
Int8 zeropoint	56.66	16.24	14.76	13.49	13.94
Int8 absmax row-wise	30.93	17.08	15.24	14.13	16.49
Int8 absmax vector-wise	35.84	16.82	14.98	14.13	16.48
Int8 zeropoint vector-wise	25.72	15.94	14.36	13.38	13.47
Int8 absmax row-wise + decomposition	30.76	16.19	14.65	13.25	12.46
Absmax LLM.int8() (vector-wise + decomp)	25.83	15.93	14.44	13.24	12.45
Zeropoint LLM.int8() (vector-wise + decomp)	25.69	15.92	14.43	13.24	12.45

Zeropoint > absmax because outliers non-symmetric (either very large or very small, but not both)

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LLM.int8(): 8-bit Matrix Multiplication for Transformers at Scale (Dettmers et al., NeurIPS 2022)

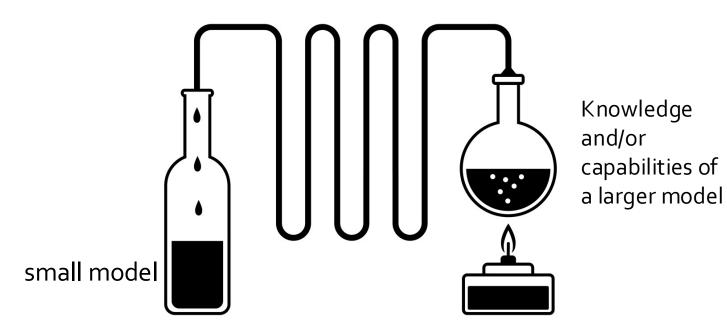
- Maps floating point numbers (fp32, fp16, bf16) to low precision numbers (fp8, int8) to save memory.
- Is effective in reducing the memory required for both training / inference.
- 8-bit quantization loses minimal performance, while 4-bit quantization is hard, can be harmful to model performance.



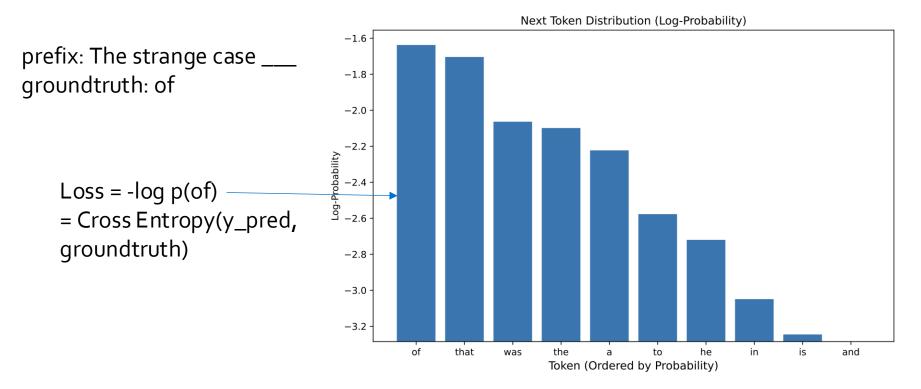
Distilling the knowledge of larger models



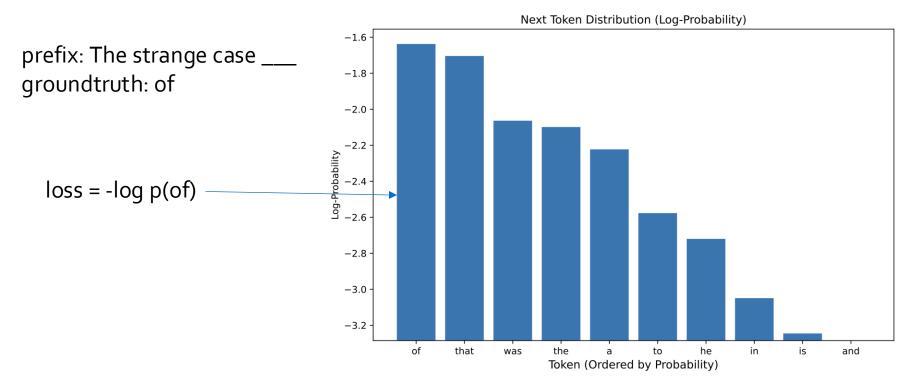
Distillation





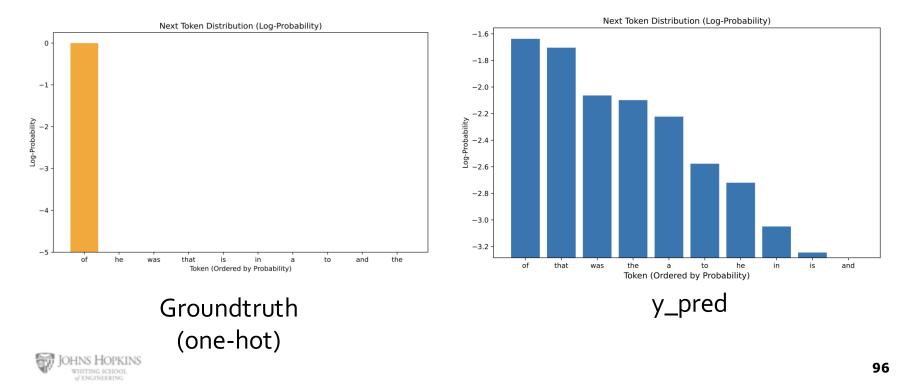




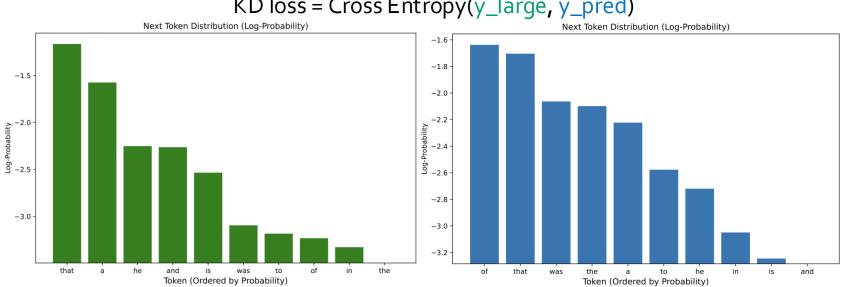




loss = -log p(of) = Cross Entropy(groundtruth, y_pred)



Knowledge Distillation



KD loss = Cross Entropy(y_large, y_pred)

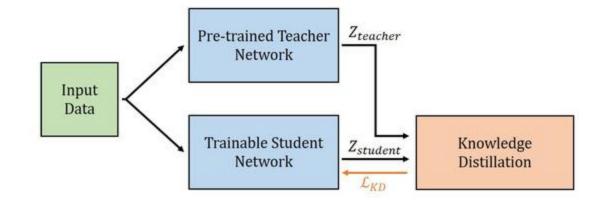
Large model next token probs (y_large)

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small model next token probs (y_pred)

Knowledge Distillation

Step 1: Initialize teacher model with a large and capable model



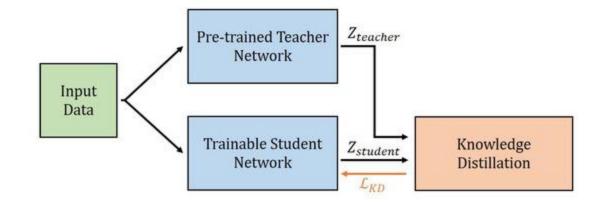
Step 2: Feed input data to both student and teacher (freezed)

> Step 3: Use teacher outputs to train student (Cross Entropy)



What if the teacher is Proprietary (GPT)?

Step 1: Initialize teacher model with a large and capable model

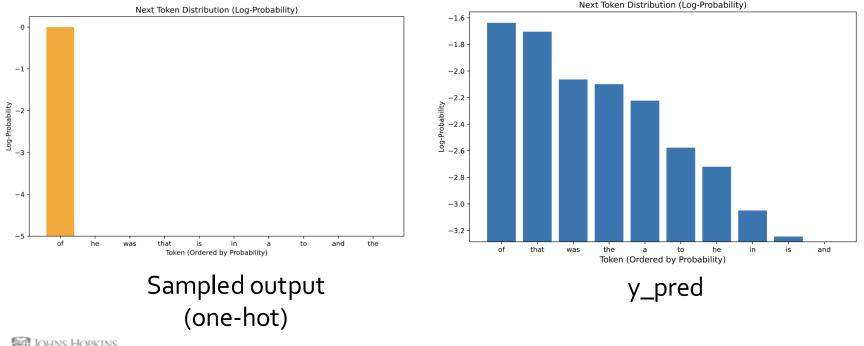


Step 2: Feed input data to both student and teacher (freezed)

> Step 3: Use teacher generations (instead of outputs) to train student!



loss = -log p(of) = Cross Entropy(sampled text, y_pred)



What works better (a study in 2016)

$BLEU_{K=1}$	$\Delta_{K=1}$	$BLEU_{K=5}$	$\Delta_{K=5}$
17.7	_	19.5	_
19.6	+1.9	19.8	+0.3
14.7	_	17.6	_
15.4	+0.7	17.7	+0.1
18.9	+4.2	19.0	+1.4
	$ 17.7 \\ 19.6 \\ 14.7 \\ 15.4 $	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

Sequence-Level Knowledge Distillation (Kim & Rush, EMNLP 2016)



Knowledge Distillation

- Train student (usually smaller model) on the output of a teacher (usually a larger model)
- The output can be log-probabilities or sampled outputs
- Effective in "distilling" the knowledge of large models to smaller ones.

